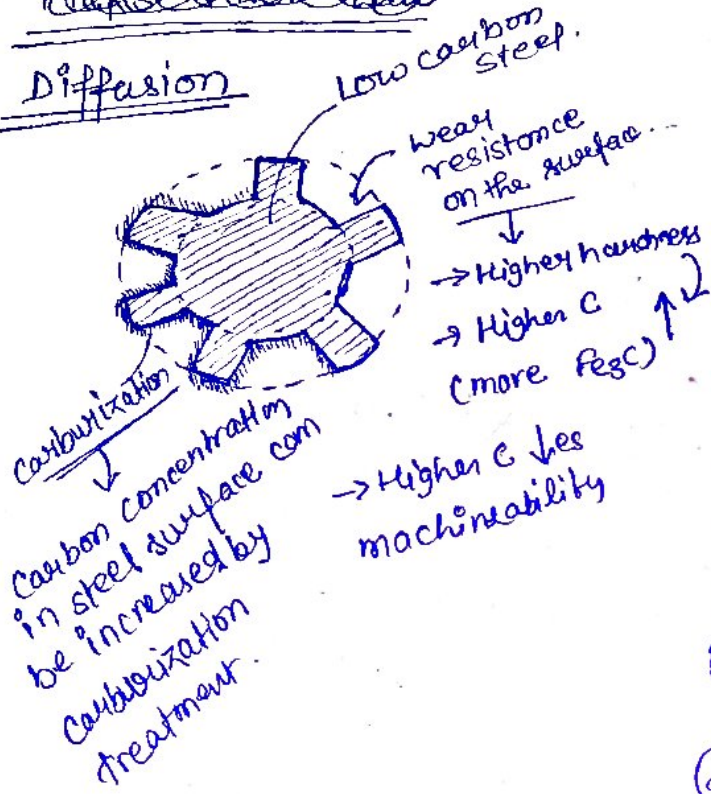


Farrell-Rust Law

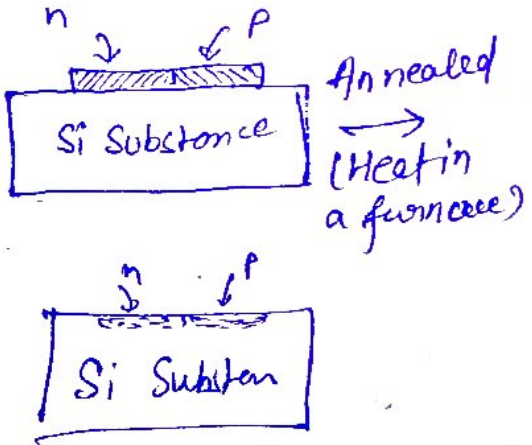
Diffusion



→ Heat the low carbon-aceous atmosphere (packing in C powder or hydrocarbon gases).

→ This is possible bcoz of diffusion.

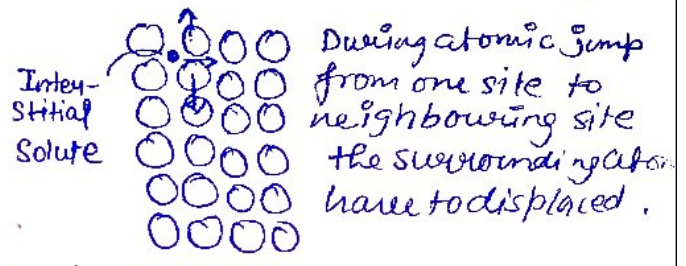
pn-Junction (example).



Two kinds of diffusion

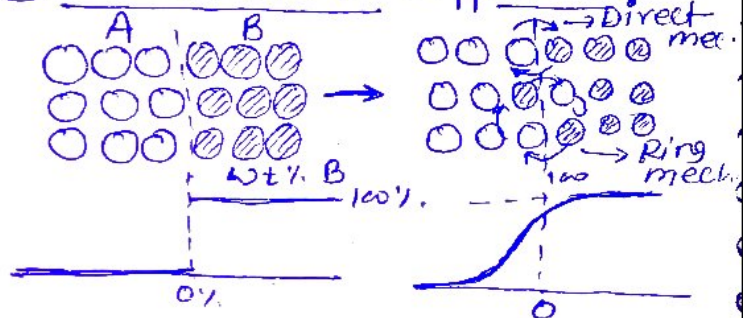
1. Interstitial Diffusion

(Diffusion of Solute in an interstitial solid solution)



→ Interstitial atoms jumps from one interstitial site to a neighbouring interstitial position.

2. Substitutional Diffusion



→ Direct/Ring/Vacancy mechanism, are made.

Note: Interstitial diffusion is generally faster than substitutional diffusion.



$$[D] = \frac{[j]}{\left[\frac{\partial c}{\partial x}\right]} = \frac{\text{kg m}^{-2} \text{s}^{-1}}{\left(\frac{\text{kg/m}^3}{\text{m}}\right)} = \text{m}^2 \text{s}^{-1}$$

$$= [M^2 T^{-1}]$$

Fick's First Law of Diffusion

	Heat Flow	charge flow	mass flow
1. Flux	Heat flux $q \text{ (J m}^{-2} \text{s}^{-1})$	charge flux $j \text{ (current density)}$	mass flux j
2. gradient	Temp. grad $\frac{\partial T}{\partial x}$	Electric Potential grad $\frac{dv}{dx}$	Concentration gradient $\left(\frac{dc}{dx}\right)$
3. Law	Fourier's Law $q = -k \left(\frac{dT}{dx}\right)$	Ohm's Law $j = -\sigma \frac{dv}{dx}$	Fick's $j = -D \left(\frac{dc}{dx}\right)$
4. Material Property	Thermal conductivity $(k) \text{ (W m}^{-1} \text{K}^{-1})$	Electrical conductivity σ	Diffusivity or Diffusion coefficient
5. year	1807	1827	1855.

- Diffusivity is highly temp. dependent.

$$- D = D_0 \exp\left(-\frac{Q}{RT}\right)$$

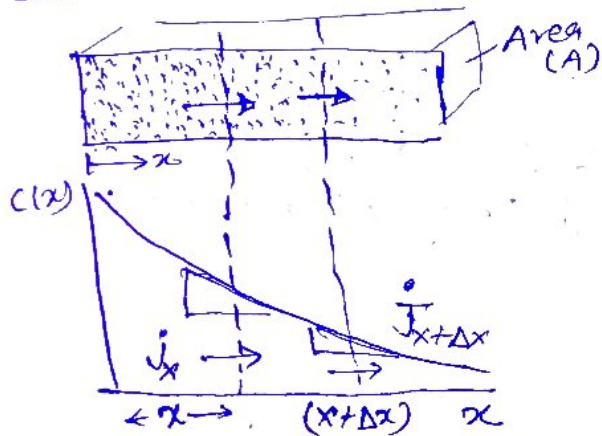
D_0 = pre exponential factor

R = Gas constant

Q = Activation Energy.

T = Abs. Temp.

Fick's Second Law



$$\text{Volume } (\Delta V) = A \cdot \Delta x$$

$$\text{mass entering} \quad m_x = j_x \cdot A \cdot \Delta t$$

$$\text{mass leaving} \quad m_{x+\Delta x} = j_{x+\Delta x} \cdot A \cdot \Delta t$$

$$j = -D \frac{\partial c}{\partial x}$$

j = mass flux.



mass flows from high concentration to low concentration region

mass accumulation

$$\Delta m = (j_x - j_{x+\Delta x}) A \cdot \Delta t$$

$$= -(\Delta j) \cdot A \cdot \Delta t$$

Concentration change in ΔV in time Δt .

$$\Delta c = \left(\frac{\Delta m}{\Delta V} \right)$$

$$= \frac{-\Delta j \cdot A \cdot \Delta t}{A \cdot \Delta x}$$

$$= -\frac{\Delta j}{\Delta x} \cdot \Delta t$$

$$\frac{\Delta c}{\Delta t} = -\frac{\Delta j}{\Delta x}$$

take limit.

$$\lim_{\Delta t \rightarrow 0} \left(\frac{\Delta c}{\Delta t} \right) = -\lim_{\Delta x \rightarrow 0} \frac{\Delta j}{\Delta x}$$

$$\boxed{\frac{\partial c}{\partial t} = -\frac{\partial j}{\partial x}} \quad \text{Fick's 1st form}$$

We can obtain another form of IInd law. by replacing j using Fick's 1st law.

$$j = -D \cdot \frac{\partial c}{\partial x}$$

$$\frac{\partial c}{\partial t} = -\frac{\partial}{\partial x} \left(-D \cdot \frac{\partial c}{\partial x} \right)$$

$$\boxed{\frac{\partial c}{\partial t} = D \left(\frac{\partial^2 c}{\partial x^2} \right)} \quad \text{Fick's II}^{\text{nd}} \text{ law 2}^{\text{nd}} \text{ form}$$

Assume D is independent of x .